Assumptions

For now, assume:

- Income of 100k gross (\$1920 weekly, say \$1200 after tax)
- I want to spend only 30% of my income on rent
- Will rent near city (say, for a range of 300-500 per week)
- Will rent out the investment property for ~500 per week
- For simplicity, assume rent from investment covers rent in city with no excess profit or cost
- Therefore, leftover income to spend on investment for rent per week = 1200 * 0.3 = 360
- Long-term interest rates of 7.25% (calculated monthly = 0.00625)
- Loan length = 25 years = 300 months

These assumptions will be tweaked later on.

Formula

Let:

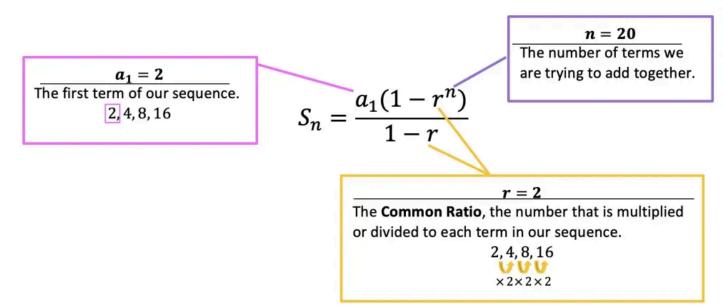
- A_n = amount owing after the nth payment
- P = principal owing
- r = interest rate calculated monthly (interest is applied before repayment)
- M = monthly repayment

$$A_1 = P + (1+r) - M$$
 $A_2 = A_1 * (1+r) - M - R = P(1+r)^2 - M(1+r) - M$ $A_3 = A_2 * (1+r) - M = P(1+r)^3 - M(1+r)^2 - M(1+r) - M$ $A_n = P(1+r)^n - M(1+r)^{n-1} - M(1+r)^{n-2} - \ldots - M$

To simplify, with every month, interest is applied and the repayment is subtracted.

As this is a geometric progression, we use the sum of a finite geometric process formula:

$$\frac{a(r^n-1)}{r-1}$$



depending on whether r is < or > 1. For us:

- a = -M
- r = 1.005 (interest rate multiplied to outstanding loan amount)
- n = number of periods

Therefore,

$$A_n=P(1+r)^n-rac{M(r^n-1)}{r-1}$$

To calculate monthly repayment, let $A_{300} = 0$ and *n* be the final period:

$$egin{aligned} rac{M(r^n-1)}{r-1} &= P(1+r)^n \ M(r^n-1) &= P(1+r)^n(r-1) \ M &= rac{P(1+r)^n(r-1)}{r^n-1} \end{aligned}$$

Calculation

Positive gearing

For a property to be positively geared, the rental yield must be more than *M*. Therefore, assuming rental yield is $500 perweek (\$500 * \frac{52}{12} = 2166.66 \text{ per month})$:

$$2167 = rac{P(1+0.00625)^{300}(1.00625-1)}{1.00625^{300}-1}
onumber \ 2167(1.00625^{300}-1) = P(1+0.00625)^{300}(1.00625-1)
onumber \ P = rac{2167(1.00625^{300}-1)}{(1+0.00625)^{300}(1.00625-1)} = 293237.6008$$

Therefore, the Principal (after putting a deposit down) must be a maximum of **\$293,237**. Even at a rental yield of \$650, the Principal must be a maximum of **\$381,195**.

Renting without using rental income at different levels of income expenditure

Now assume that I do not want to spend more than

 $340 perweekas peroriginal assumption (or $340 * <math>\frac{52}{12} = 1473.33$ per month) on repayments. Therefore, the max P I should take on is:

$$egin{aligned} &1473 = rac{P(1+0.00625)^{300}(1.00625-1)}{1.00625^{300}-1} \ &1473(1.00625^{300}-1) = P(1+0.00625)^{300}(1.00625-1) \ &P = rac{1473(1.00625^{300}-1)}{(1+0.00625)^{300}(1.00625-1)} = 199325.7896 \end{aligned}$$

Looks like I can't buy jack shit with my assumptions – **\$199,325** is not enough for Australian property. I need to relax my *leftover income to spend on investment for rent per week \$=1200*0.3=360*** assumption.

Let's say I'm willing to spend 50% of my income for this investment for rent:

$$egin{aligned} 1200*0.5&=600\ &600*rac{52}{12}&=2600\ &2600&=rac{P(1+0.00625)^{300}(1.00625-1)}{1.00625^{300}-1}\ &2600(1.00625^{300}-1)&=P(1+0.00625)^{300}(1.00625-1)\ &P&=rac{2600(1.00625^{300}-1)}{(1+0.00625)^{300}(1.00625-1)}&=351830.9931 \end{aligned}$$

Even with 50% of my income, I can't spend more than \$351,830 on a property.

Finally, let's try with 70% of my income, which is probably most realistic given I'll only need 30% of my income for spending (as per current spending habits - see <u>20231209 Savings report</u>):

$$\begin{split} 1200*0.7 &= 840 \\ 840*\frac{52}{12} &= 3640 \\ 3640 &= \frac{P(1+0.00625)^{300}(1.00625-1)}{1.00625^{300}-1} \\ 3640(1.00625^{300}-1) &= P(1+0.00625)^{300}(1.00625-1) \\ P &= \frac{3640(1.00625^{300}-1)}{(1+0.00625)^{300}(1.00625-1)} = 492563.3904 \end{split}$$

Here, I can only buy an investment for **\$492,563**.

Renting using rental income at 70% of income expenditure

Another variation to consider is that my rental income from the investment is likely to be more than my rental payments as I would live with a roommate. For simplicity, assume that the rental yield is double my rental payments (as I now live with one other roommate). Our monthly repayments can now incorporate half of the rental yield of the investment property (500 * 0.5 = 250).

Therefore, we can add 250 to the value of M:

$$250 + 1200 * 0.7 = 1090$$

 $1090 * rac{52}{12} = 4723.333333$
 $4723 = rac{P(1 + 0.00625)^{300}(1.00625 - 1)}{1.00625^{300} - 1}$
 $4723(1.00625^{300} - 1) = P(1 + 0.00625)^{300}(1.00625 - 1))$
 $P = rac{4723(1.00625^{300} - 1)}{(1 + 0.00625)^{300}(1.00625 - 1))} = 639114.531$

Results

To generalise the above, I cannot spend more than \$640,000 on an investment property assuming:

- 1. interest rates remain high;
- 2. income remains at \$100k gross; and
- 3. I live with housemates.

Discussion

From an opportunity cost perspective, purchasing a property will redirect 70% of my income, crowding out all other investment ventures. Property is not liquid, and I cannot live as freely as I do now. Property investing also primarily relies on your ability to generate income – the golden handcuffs would shackle fast.

Property is unique for its leveraging effect – you can use equity in a house to buy more property. You are likely to produce 8% growth over the long run, and the rental yield means you can live off passive income with multiple properties.

However, property investing is a game of decades. For now, I do not want to overleverage myself. I'd like to have freedom in liquidity to deploy capital in other entrepreneurial ventures.

In Australia, there are two primary incentives to purchase property investments:

- Capital Gains Tax discount; and
- tax deductions on negatively geared properties.

Therefore, once I start making a high income, I'll probably buy a property purely to minimise taxable income and hopefully sell the property with minimal CGT.

Sources

• Eddie Woo on calculating loan repayments